



Anomaly Ensembles

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 **Problem statement**

 **Item Response Theory**

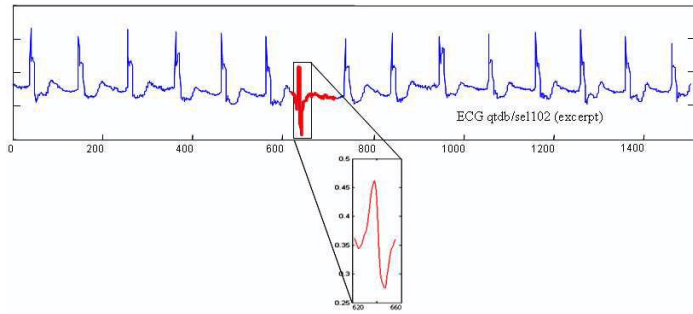
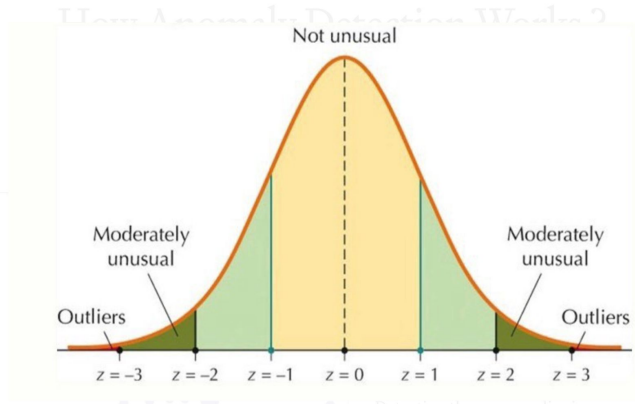
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? Problem statement

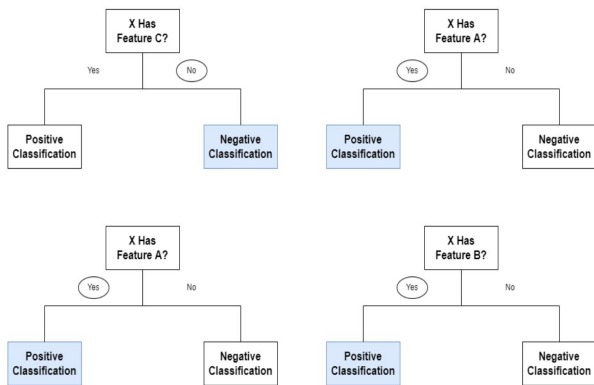


- Anomaly detection - Identifying outliers
- Example: Left and right tails in a Normal distribution
- Several everyday application: Fraud detection, fault detection, defect detection etc.
- Main focus: Identify deviations from a “normal” data set.

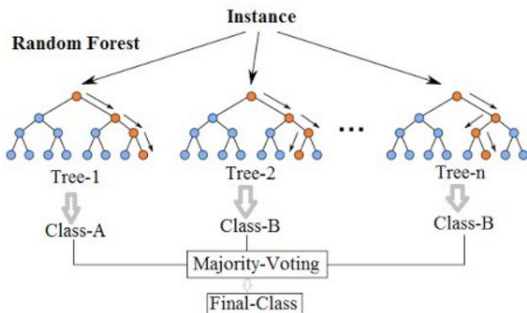


Solution: Ensembles

Ensemble Assessing Sample X



Random Forest Simplified



- Combine several base models to produce one optimal model
- Bagging, stacking, boosting
- Example
 - Decision trees, Random forests etc.

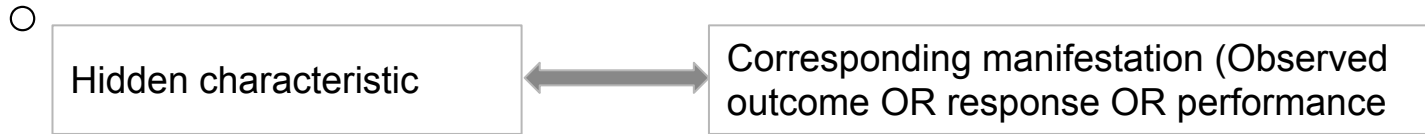
?: Challenge: Anomalies i.e. the class truth OR ground label - **unknown!**

Need: Class labels

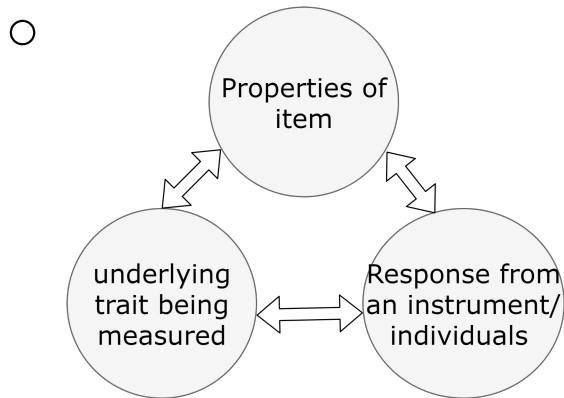


Item response theory

- Models the ground truth as a latent trait (unobservable characteristic or attribute).
- Explains the relationship between



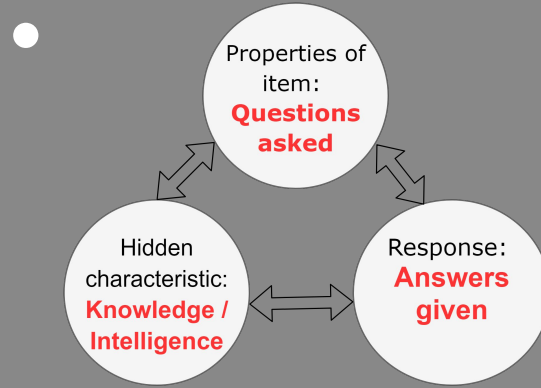
- Establishes a link between



⚡ Item response theory



- Psychometrics - Root of IRT
- Classic example:
Examination

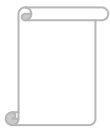


- Extend the concept to
anomaly detection

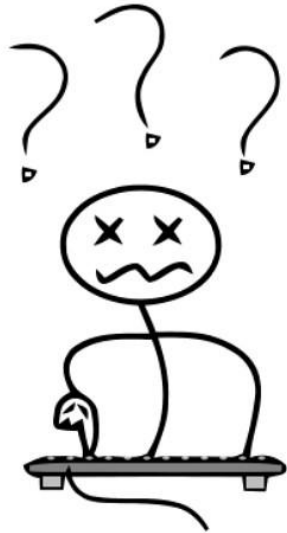


Item response theory

- Earlier researches: AD as Supervised machine learning models that used pseudo-ground-truth labels
 - Limitations: Circular argument
- Current research: IRT ensembles for unsupervised anomaly detection.
 - Latent trait: Uncover the ground truth
- IRT framework in the paper also uses - different combination functions like average, maximum and other correlation based functions on the set of the heterogenous anomaly methods.
- This paper implements unsupervised anomaly detection using combination function on ensemble

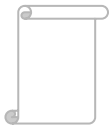


Summarising AD & IRT



Several keywords in previous slide!!

- Anomaly detection?
- Unsupervised anomaly detection?
- Unsupervised anomaly detection using ensemble!?
- Combination function?
- Unsupervised anomaly detection using combination function on ensemble!?



Summarising AD & IRT

- **Anomaly detection:** *Identifying the outliers*
- **Unsupervised Anomaly detection:** *Identifying the outliers when the ground truth is unknown*
- **Unsupervised anomaly detection using ensembles**
 - *Unsupervised Anomaly Detection (AD) methods - gives - “anomaly scores” for each observation in the dataset*
 - *Larger scores - anomalous observations.*
 - *Ensemble scores = combination of normalised anomaly scores from several methods*

Ensemble score in unsupervised AD using ensembles

Ensemble
score

=

Anomaly
score 1

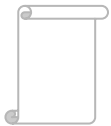
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Anomaly
score 2

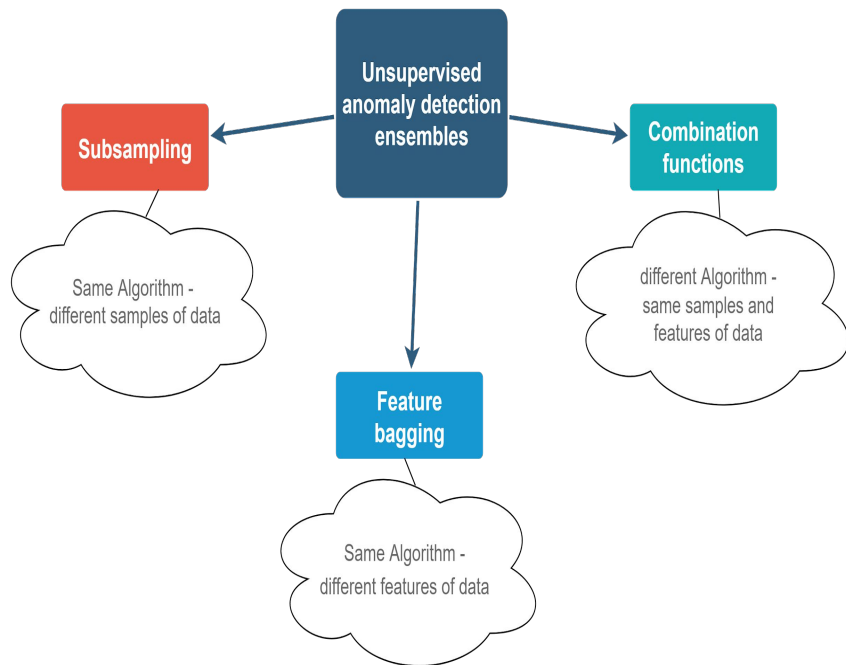
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...

Anomaly
score n

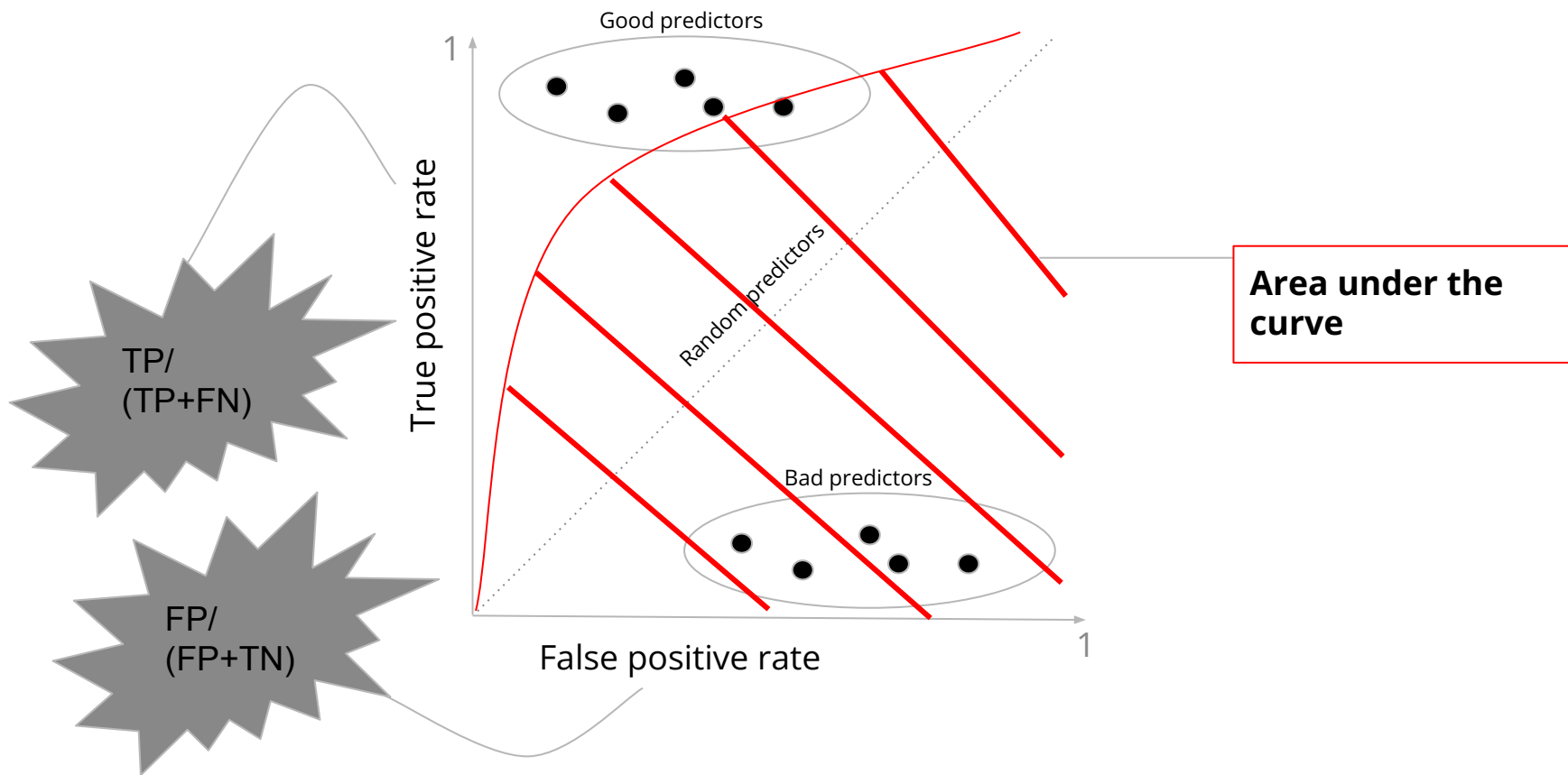


Summarising AD & IRT



- **Combination function:** *One from the flow chart*
- **Unsupervised anomaly detection using combination function on ensemble:**
 - *Used in this research.*
 - Anomaly scores - by several different methods. Ex: LOF - density based outlier with decisions based on LOF score
 - Ensemble score by - *combination functions like average, greedy, averaged greedy, ICWA, Max, thresh along with IRT.*
 - *Best performing combination function as per ROC is analysed.*

Quick recap on ROC



More on algorithms & implementation

Average

- Computes average anomaly score
- Pro: Benchmark, performs well in homogeneous data distribution
- Cons: Subpar performance in heterogeneous data

Greedy

- If something works, we favor it more.
- Selects best methods - using correlation and K number of anomalies
- Pro: able to handle correlation
- Cons: slower than average, might not arrive at optimal solution

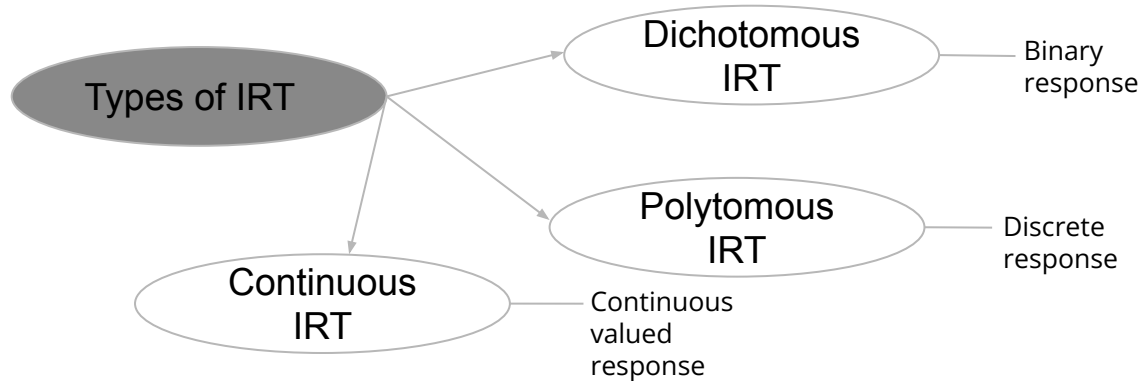
Many more combination functions



More on algorithms & implementation

IRT

- From earlier slides: latent trait model, fitted using responses. There are several types of IRT based on the responses used in fitting



- Look deep into - Dichotomous IRT

More on algorithms & implementation

$$\Phi(y_{ij} = 1 | \theta_i, \alpha_j, \beta_j) = \frac{1}{1 + \exp(-\alpha_j (\theta_i - \beta_j))} .$$

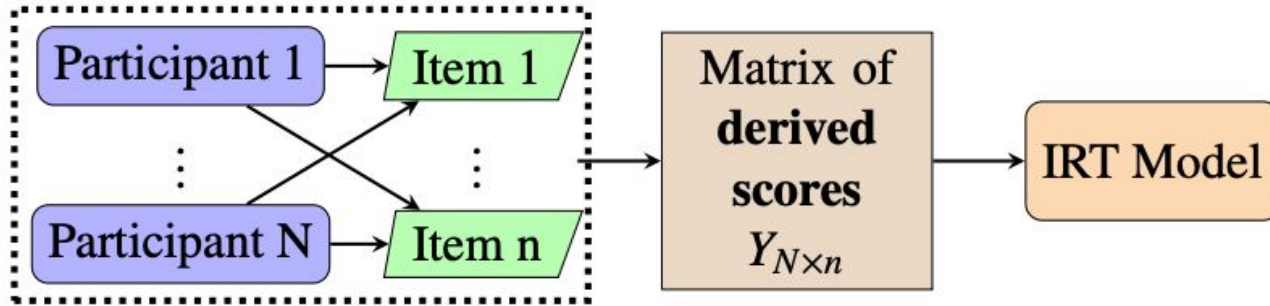


- **Assume:**
 - $i = 1, 2, \dots, N$ participants
 - $j = 1, 2, \dots, n$ test items
 - $Y_{\{ij\}} \in \{0, 1\}$ - score or response of the i th participant to the j th test item
- **Parameters:**
 - Discrimination parameter $\alpha_{\{j\}}$
 - difficulty parameter by $\beta_{\{j\}}$
- **Equation and 2-Parameter**
← **Logistic (2PL) mode as shown.**
 $\theta_{\{i\}}$ is ability.
- **Note: When $\alpha_{\{j\}} = \beta_{\{j\}}$, , $\Phi = 0.5$**

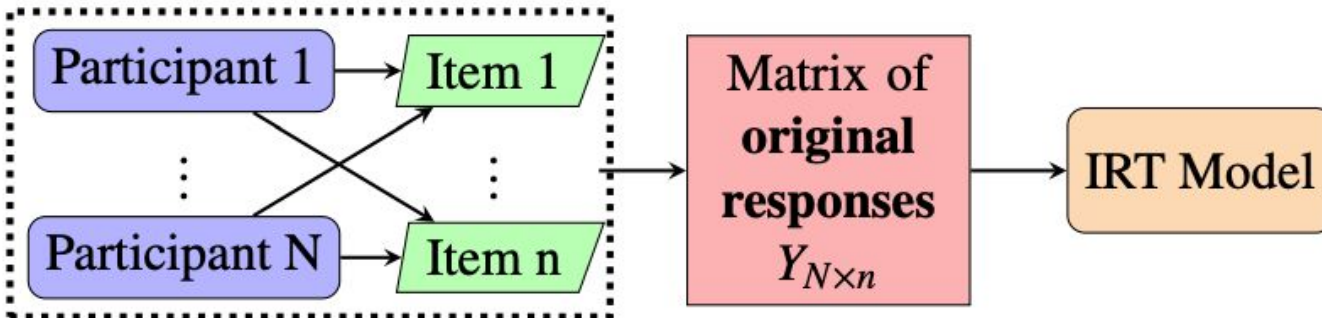
Mapping IRT to ensemble

- Two possibilities of mapping the response in psychometrics

1



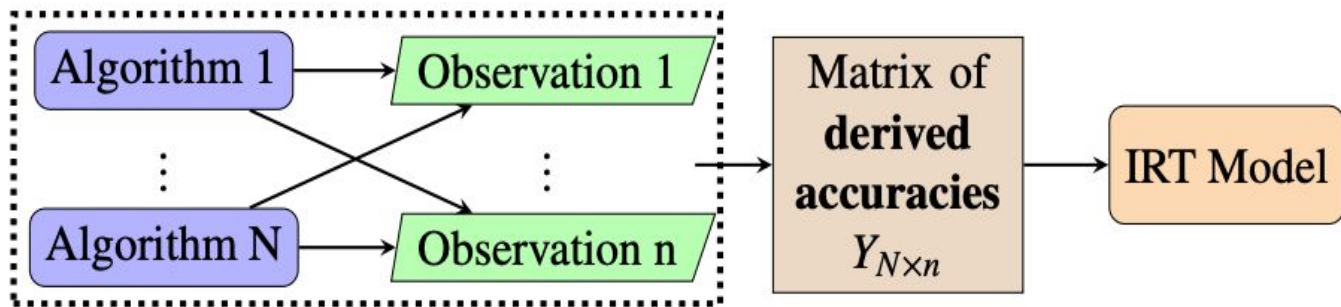
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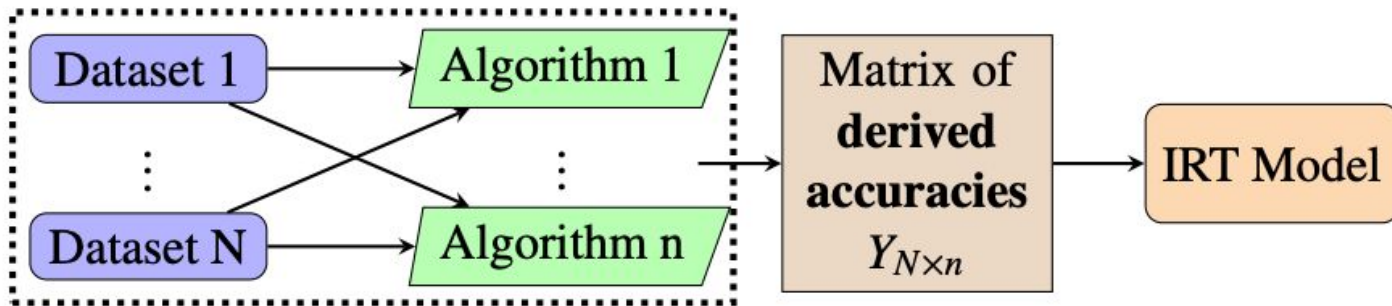
Mapping IRT to ensemble

- Two possibilities of algorithm evaluation

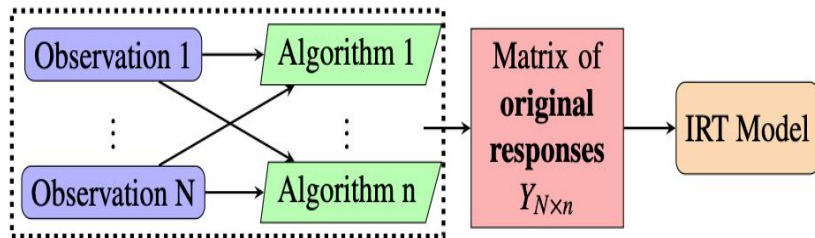
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2



Mapping IRT to ensemble

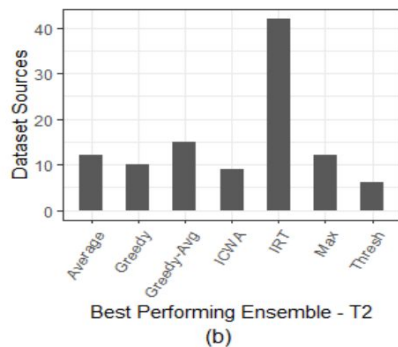
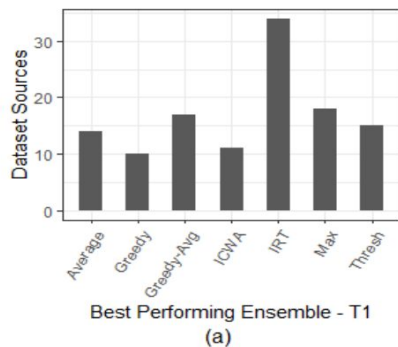
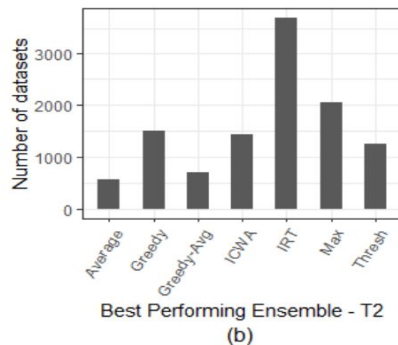
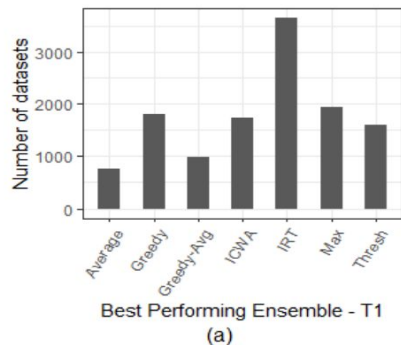


- **Current research - Mixture of both**
- **Uses Standardised Original responses instead of an accuracy measure.**
- **Maps participants to dataset observations and test items to algorithms.**



Experiments in Ensemble

Results:



- **Data set:**
 - 12433 publicly available anomaly detection datasets
 - prepared from 119 source datasets
 - minority class is considered anomalous
- **Methods:** *KNN-AGG, LOF, COF, INFLO, KDEOS, LDF and LDOF*
- **Combination functions:** *average, greedy, averaged greedy, ICWA, Max, thresh, IRT.*
- **Parameter Setting:**
 - *T1: default values for $k = k_{min} = 5$ and $k_{max} = 10$*
 - *T2: $k = k_{min} = \max(N/10, 50)$ and $k_{max} = k + 10$*
- **Performance evaluation:** *AUC*



Conclusion and improvements

Conclusion

- In unsupervised learning - constructing ensemble using heterogeneous AD methods - challenge
- Introduced - IRT - uses latent trait to compute the ground truth for the first time.
- Evaluated the IRT ensemble w.r.t. 6 other AD ensemble techniques. Result - IRT performs the best

Improvements

- When and why ensembles work - is not explained
- Can justify more on the base models used
- Harder to justify Ensemble results
- AUC is a basic performance evaluator. Does not compare anomaly scores.
- IRT & Ensembles in general is computationally expensive.

References

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Thank you !